## Engineering Economic Analysis

- Engineering Economy deals with the concepts and techniques for evaluating the worth of systems, products, and services in relation to their costs.


## Engineering Economic Analysis

- It is used to answer many different questions
- Which engineering projects are worthwhile?
- Has the design engineer shown that the solar tracker project he designed is worth developing?
- Which engineering projects should have a higher priority?
- Has the construction engineer shown which road improvement projects should be funded with the available dollars?
- How should the engineering project be designed?
- Has the electronics engineer chosen the best material for fiber optic insulation?


## Outline

- Time Value of Money
- Interest
- Cash Flow Diagrams
- Evaluating Economic Alternatives
- Present Worth Analysis
- Annual Equivalent Worth
- Breakeven Analysis


## Elements of a Transaction

- $P=$ Principal (Amount of money invested)
- P can also be the Present Worth of an investment
- i = Interest rate (The cost of money)
- N= Duration of the transaction
- A= Amount in a regular series of payments
- A can also be an annual cost or revenue
- F= Future amount


## Time Value of Money

- Money has value
- Money can be leased or rented
- The payment is called interest

- If you put $\mathbf{\$ 1 , 0 0 0}$ in a bank at $\mathbf{1 0 \%}$ interest for one time period you will receive back your original $\mathbf{\$ 1 , 0 0 0}$ plus $\mathbf{\$ 1 0 0}$

Original amount to be returned $=\$ 1000$ Interest gained $=\$ 1,000 \times .1=\$ 100$

For simplicity, interest will be considered inflation-adjusted

## Compound Interest

- Interest that is computed on the principal (original unpaid debt) and the unpaid interest
- Compound interest is most commonly used in practice
- Total interest earned $=I_{N}=P(1+i)^{N}-P$
- Where,
- P - present sum of money
- i - interest rate
- $N$ - number of periods (years)


## Cash Flow

- Engineering projects generally have economic consequences that occur over an extended period of time
- For example, if an expensive piece of machinery is installed in a plant were bought on credit, the simple process of paying for it may take several years
- Each project is described as cash receipts or disbursements (expenses) at different points in time.


## Categories of Cash Flows

- The expenses and receipts due to engineering projects usually fall into one of the following categories:
- Initial cost [-]: expense to build or to buy and install
- Operations and Maintenance (O\&M) [-]: annual expense, such as electricity, labor, and minor repairs
- Salvage Value [+]: receipt at project termination for sale or transfer of the equipment
- Revenues [+]: annual receipts due to sale of products or services
- Overhaul [-]: major capital expenditure that occurs during the asset's life


## Cash Flow Diagram (CFD)

- A CFD is created by first drawing a segmented time-based horizontal line, divided into appropriate time unit. Each time when there is a cash flow, a vertical arrow is added - pointing down for costs [-] and up for revenues or benefits [+]. The cost flows are drawn to relative scale


## An example of a Cash Flow Diagram



Borrower's Perspective

## Future Worth and Present Worth

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- Future Worth (F)
- If you deposit $P$ dollars today for $N$ periods at $i$, you will have $F$ dollars at

$$
F=P(1+i)^{N}
$$ the end of period $N$.

- Present Worth (P)
- $F$ dollars at the end of period $N$ is equal to a single sum $P$ dollars now, if your earning power is measured in terms of interest rate $i$.


## Evaluating Economic Alternatives

## Measures of Investment Worth

Annual Equivalent Worth (AE) Analysis
Net Present Worth (NPW) Analysis
Breakeven Analysis

## Annual Equivalent Analysis

## Annual Equivalent Worth (AEW)

## AEW = Annual Equivalent Benefits $\boldsymbol{-}$ Annual Equivalent Costs

For a project to be economically feasible, Revenues must exceed costs.

Two main kinds of costs:
Operating costs and capital costs

## Choosing alternatives using Present Worth

Which of these two alternatives would you choose if the interest rate is $\mathbf{8 \%}$ ?

| Year | Plan 1 | Plan 2 |
| :---: | :---: | :---: |
| 0 |  | $\$ 5,000$ |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 | $\$ 5,000$ | $\$ 5,000$ |
| Total | $\$ 000$ |  |

To make a choice the cash flows must be altered so a comparison may be made.

## An example of Net Present Worth Calculation

- It has been projected that a design project for a garage door remote sensor will yield a revenue of $\$ 60,000$ after 5 years. If initial costs total $\$ 15,000$, compute its net present worth at an interest rate of $10 \%$.
- Solution:
- The Net Present Worth = Present equivalent of revenue (benefit) - Initial cost
- Find Peq; Given F=\$60,000, $\mathrm{N}=\mathbf{5}, \mathrm{I}=\mathbf{1 0 \%}$
- $\operatorname{Peq}=F(1+i)^{-N}=60,000(1.1)^{-5}=37,255$
- $N P W=37,255-15,000=\$ 22,255$


## Breakeven Analysis

- Breakeven analysis is commonly used to study relationships among costs, revenue, and volume:
- Define cost and revenue functions
- Linear (or non-linear) functions of volume, price, etc.
- Objective: Find the value (volume, price, etc.) that maximizes profits


## Fixed Costs (FC)

- Do not vary with production or activity levels, price, etc.
- Examples:
- Buildings
- Insurance
- Fixed overhead
- Equipment
- etc.


## Variable Costs (VC)

- Vary with the level of activity
- Examples:
- Direct labor (wages)
- Materials
- Indirect costs (e.g., fringe benefits)
- Marketing
- Advertising
- Warranty
- etc.


## Breakeven Analysis



- Revenue (R)
- Total Cost (TC):
- Fixed Cost (FC)
- Variable Cost (VC)

$$
T C=F C+V C
$$

- At the breakeven point:

$$
\mathrm{R}=\mathrm{TC}
$$

- Profit:
- Revenue minus total cost
Profit = R - TC

In per unit terms, the breakeven quantity of units

$$
q^{*}=\frac{F C}{r-v}
$$

$r$ is the revenue per unit, $v$ is the variable cost per unit

## Practice Problem: Breakeven Analysis

Star Design Group invested $\mathbf{\$ 4 , 0 0 0 , 0 0 0}$ as fixed cost in a project. The variable cost was $\$ 2,000,000$ per year. If the total revenue is at a rate of $\$ 3,000,000$ per year. Calculate the breakeven point, in years.

## Summary

- Engineering economic analysis should consider the time value of money
- The Present Worth method can be used to evaluate alternatives having different lives
- The Annual Equivalent method has the advantage of not requiring the use of the least common multiple.
- The breakeven point is the level of production (and sales) that results in a zero profit

